

PHYS 4330 Theoretical Mechanics

Homework # 2

Submission deadline: 23 January 2024 at 11:59 pm Eastern Time

Submission Instructions: Homework is submitted on Gradescope to Homework 2.

1. A meter stick is at rest in reference frame S_0 , which is traveling relative to reference frame S with speed $v=0.75c$ in the positive x -direction of S . *[This is the setup for both parts (a) and (b)].*

- (a) The stick lies in the x_0, y_0 plane and makes an angle $\theta_0=45^\circ$ with the x_0 axis (as measured in S_0 .) What is the length l of the meter stick as measured in S , and what is its angle θ with the x -axis?
- (b) Now assume that you measure an angle of $\theta=45^\circ$ in S . What is θ_0 for this to happen? What is the value of l , as measured in S now?

[10 points]

2. A rocket is traveling at speed $V=0.95c$ along the x -axis of frame S . It shoots a bullet whose velocity \mathbf{v}' (measured in the rocket's rest frame S') is $v_y'=0.9c$ along the y' axis of S' . *[Assume that the x and x' axes are aligned as are the y and y' axes.]*

- (a) **Derive** the equation for x and y velocities in the S' reference frame (v_x' and v_y') in terms of the velocity in the S frame and V .
- (b) Calculate the individual velocity components in the S frame and report the bullet's total velocity (magnitude and direction) as measured in S ?

[10 points]

3. Cosmic rays create muons in the Earth's upper atmosphere. These muons rain down more-or-less uniformly on the Earth's surface, although some of them decay on the way to the surface, with a half-life of $\sim 1.5 \mu\text{s}$ (measured in their rest frame). A muon detector is carried in a balloon to an altitude of 2000 m, and in the course of an hour detects 650 muons traveling at $0.99c$ toward the Earth.

- (a) What is the muon's half-life as measured by an observer on the surface of the Earth?
- (b) If an identical detector remains at sea level, how many muons should it register in one hour?
- (c) What would the answer be if you ignore the effects of time dilation?

[10 points]